## Toward Developing a Regional IFC Forest Productivity Model



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## Summary

- Background
- Individual tree analysis
  - RF
  - Linear models
- Whole stand productivity
- Stand subset productivity
- Challenges
- Conclusions / future directions

## Background

- What is Site Productivity?
- Productivity can be directly measured
  - Volume growth/acre/year
- Site Productivity is a little more tricky . . .
  - Volume growth/acre/year the site is capable of producing
    - Difficult to directly measure



# Background

- Proxies are often used for site productivity
  - Site index
  - Habitat type

- Site productivity is very useful
  - Growth and yield models
  - Land appraisals
  - Management strategies



# Background

### Growth and Yield Models

- Many use individual tree models
  - Diameter growth
  - Volume growth
  - FVS
- Whole stand models
  - Less common
  - Ultimate goal of G & Y models



# The Dataset

- Repeated growth measurements (CFI)
- Primarily Northern ID
- Variety of owners
  - USFS
  - IDL
  - Potlatch
  - Etc.



Figure 1: Sample plot locations

# The Dataset

- 4589 Unique Stands / Plots
- Over 1,000,000 Individual tree observations
- Initially . . .
- Much is lost after data screening



Figure 1: Sample plot locations

# Phase 1: Individual Tree

- Response Variable
  - InDDS
    - "…Logarithm of the change in squared insidebark individual tree diameter over a period of 10 years…"
  - Use<mark>d</mark> in FVS
- 110,852 individual tree observations
- Model selection methods
  - Random Forests (RF, Breiman 2001)
  - Best R<sup>2</sup>

## **Random Forests Models**

- Builds multiple regression trees
- Rank explanatory variables on influence / importance
- Examines:
  - Increase in Mean Squared Error
  - Node purity
    - Decrease in residual sum of squares
    - Averaged over all the trees



### **Random Forests Models**

### Four models

- rf1: all predictors were included
- rf2: just site predictors
- rf3: rf2 plus Species and cr.
- rf4: traditional variables used in FVS

Table 9: Summary	of the	RF	models
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RF model	R2	Best 10 predictors
rf1	0.84	DBH, cr, Species, soilcd, TopHt, baldbh, QMD, pratio, BAPctile, Slope
rf2	0.39	slca, slsa, soilcd, pratio, ffp, smrsprpb, map, Geology, gsp, winp
rf3	0.54	Species, cr, pratio, slca, slsa, winp, soilcd, map, adi, Geology
rf4	0.83	cr, Species, DBH, TopHt, elev, slca, baldbh, BAPctile, QMD, PtBAL

### RF 1

• rf1: all predictors were included

Variable	Description
DBH	Diameter breast height
Species	Tree species
cr	Crown ratio
soilcd	Soil class names
pratio	Ratio of summer precipitation to total precipitation
TopHt	Height of the largest 40 trees per acre in the stand
	Interaction between DBH and Ratio of basal area in trees larger than
baldbh	subject tree (bal)
QMD	Quadratic mean diameter
BAPctile	Percentile point in the distribution of tree basal areas
Slope	Slope percentage

#### Table 9: Summary of the RF models

RF model R2 Best 10 predictors

rf1 0.84 DBH, cr, Species, soilcd, TopHt, baldbh, QMD, pratio, BAPctile, Slope

## Phase 1: Individual Tree

### **Explanatory Variables**

• Species

### Table 1: Species codes, names, and observation counts

FVSCode	Common Name	Name	Frequency
AF	subalpine fir	Abies lasiocarpa	3085
DF	Douglas-fir	Pseudotsuga menziesii	24769
ES	Engelmann spruce	Picea engelmannii	3383
GF	grand fir	Abies grandis	23314
LP	lodgepole pine	Pinus contorta	5520
MH	mountain hemlock	Tsuga mertensiana	1986
PP	ponderosa pine	Pinus ponderosa	2477
RC	western redcedar	Thuja plicata	13465
WH	western hemlock	Tsuga heterophylla	8686
WL	western larch	Larix occidentalis	7481
WP	western white pine	Pinus monticola	16701

## Phase 1: Individual Tree

### Soil class names (soilcd)

Table 2: Soil class names (soiled) and observation counts

Soil class name	Frequency
Basalt	155
Glacial	1427
Loess	261
LoessBasalt	803
LoessMetaGranite	1001
Metased	426
Other	331
Seds	1180
VolcanicBasalt	166
VolcanicGlacial	7901
VolcanicLoess	2696
VolcanicLoessBasalt	2814
VolcanicLoessGlacial	8156
VolcanicLoessMetaGranite	3540
VolcanicLoessMetased	523
VolcanicLoessOther	239
VolcanicLoessQuartzite	1209
VolcanicMetaGranite	16208
VolcanicMetased	41667
VolcanicOther	408
VolcanicQuartzite	4919
VolcanicSeds	14822

### • rf2: just site predictors

Variable	Description
slca	Slope * cos(pi/180*Aspect)
slsa	Slope * sin(pi/180*Aspect)
soilcd	Soil class names
pratio	Ratio of summer precip to total precip
ffp	Frost free period
smrsprpb	Summer spring precipitation balance
winp	Winter precipitation
map	Mean annual precipitation
Geology	Parent material
gsp	Growing season precipitation

#### Table 9: Summary of the RF models

RF model R2 Best 10 predictors

rf2 0.39 slca, slsa, soilcd, pratio, ffp, smrsprpb, map, Geology, gsp, winp

• rf3: rf2 plus Species and cr.

Variable	Description
slca	Slope * cos(pi/180*Aspect)
Species	Tree species
cr	Crown ratio
slsa	Slope * sin(pi/180*Aspect)
soilcd	Soil class names
pratio	Ratio of summer precip to total precip
winp	Winter precipitation
map	Mean annual precipitation
Geology	Parent material
adi	Annual dryness index

#### Table 9: Summary of the RF models

RF model R2 Best 10 predictors

rf3 0.54 Species, cr, pratio, slca, slsa, winp, soilcd, map, adi, Geology

Geology

### Table 3: Geology variable frequencies

Geology	Frequency
CaMetased	24464
Extrusive	4895
Glacial	10497
Intrusive	18375
Metasedimentary	44045
Other	8467
Sedimentary	109

Table 9: Summary of the RF models

RF model R2 Best 10 predictors

rf3 0.54 Species, cr, pratio, slca, slsa, winp, soilcd, map, adi, Geology

### RF 4

### rf4: traditional variables used in FVS

Variable	Description
DBH	Diameter breast height
slca	Slope * cos(pi/180*Aspect)
Species	Tree species
cr	Crown ratio
TopHt	Height of the largest 40 trees per acre in the stand
elev	Elevation
	Interaction between DBH and Ratio of basal area in trees
baldbh	larger than subject tree (bal)
QMD	Quadratic mean diameter
BAPctile	Percentile point in the distribution of tree basal areas
	Basal area per acre in larger trees measured on the
PtBAL	subplot same as BAL if there is one plot

#### Table 9: Summary of the RF models

RF model	R2	Best 10 predictors
rf4	0.83	cr, Species, DBH, TopHt, elev, slca, baldbh, BAPctile, QMD, PtBAL

### **RF Model Summary**



Phase 2: Individual Tree

- Linear and mixed effects models
- Selected based on RF models
- Best model R<sup>2</sup>
- 2 best models presented here

Table 11: Two sequences of adding variables to the lme models[ R2 is reported without random effect

R2 Predictors

```
Sequence 1, adding tree metrics
0.65 Species + soilcd + Species:cr + slca + slsa + pratio + map +
Species:adi +
I(log(DBH)) + I(DBH*DBH) + bal + Species:baldbh
Sequence 2, adding site metrics
0.64 Species + Species:cr + I(log(DBH)) + I(DBH*DBH) + bal +
Species:baldbh + soilcd + slca + slsa + pratio + map
```

## Phase 2: Individual Tree



	•	
Linear model	R2	R2 when predictions include random "StandID" effect
lm1	0.23	n/a
lme1	0.10	0.48
lm2	0.69	n/a
lme2	0.65	0.82
lme3	0.64	0.82
lme4	0.64	0.82

Table 10: Pseudo-R-square (R2) values for the linear models in table 8

- All models tested here
- Random "StandID" effect explaining a lot of variation
  - Not explained by other variables

# Individual Tree Conclusions

- Growth models can benefit from including soil and climate data
- Stand and tree characteristics often out-weight site characteristics
  - Site characteristics are indirectly incorporated in stand and tree measurements
- Quantifying inter-tree competition was difficult on large fixed area plots
  - "StandID" effect?
- Whole stand productivity could be explored.

- Same data set
- Summarized and examined in different ways
- 4,308 stands initially
- 12% 20% available after screening
  - Stands that were treated with fertilizer
  - Negative or 0 growth

Data Summaries

- DBH, Height, Volume calculated for every tree
- Every measurement period
- Expanded to a per acre value
- Means for each stand to represent productivity
- Standardized to per year
  - Different measurement period lengths

### Model and Variable selection

- 3 parts
- First chose model with the best fit via AICC selection
- Removed insignificant variables ( $\alpha < 0.1$ )
- Tested interactions between significant variables

- Whole stand volume growth (ft<sup>3</sup>/acre/year)
- Including everything . . .  $R^2 = 0.56!$

Response: mean. vol. growth. yr					
-	Sum Sq	Df	F value	Pr(>F)	
(Intercept)	571	1	0. 2718	0.6024906	
El evFt	32129	1	15. 2918	0.0001115	* * *
cub.ft.acre	70483	1	33. 5467	1.599e-08	* * *
qmd	38516	1	18. 3319	2.425e-05	* * *
logit.shade	8338	1	3.9684	0.0471717	*
El evFt: DEM_Sl opePct	21862	1	10.4052	0.0013802	* *
DEM_Sl opePct: tp. acre	27307	1	12.9969	0.0003593	* * *
cub. ft. acre: SlopePct	36598	1	17.4190	3.823e-05	* * *
cub.ft.acre:DF_SI	92848	1	44. 1915	1.205e-10	* * *
cub.ft.acre:tp.acre	19223	1	9. 1494	0.0026797	* *
qmd: Mat	12258	1	5.8341	0.0162520	*
qmd: DEM_Sl opePct	30280	1	14.4120	0.0001742	* * *
DEM_Sl opePct: curt. rd	10578	1	5.0347	0. 0254955	*
DF_SI:curt.rd	94144	1	44.8085	9.125e-11	* * *
cub.ft.acre:curt.rd	46801	1	22.2754	3. 472e-06	* * *
qmd: curt. rd	33538	1	15.9626	7.942e-05	* * *
DF_SI: sdi	104879	1	49.9178	9. 293e-12	* * *
cub.ft.acre:sdi	44641	1	21.2471	5.743e-06	* * *
logit. shade: Mat	16244	1	7.7316	0.0057323	* *
El evFt: l ogi t. shade	7880	1	3.7506	0.0536270	•
qmd:logit.shade	21468	1	10.2178	0.0015230	* *
logit. shade: curt. rd	26262	1	12.4995	0.0004642	* * *
l ogi t. shade: sdi	25508	1	12.1405	0.0005587	* * *
$\operatorname{Resi}$ dual s	705946	336			

- Got a little messy
- Just look at site factors . . . R<sup>2</sup> = 0.09

Coefficients:Estimate Std. Error t value Pr(>|t|)(Intercept)1000.98241162.985536.1421.45e-09\*\*\*dd5-0.292770.05517-5.3061.55e-07\*\*\*smrsprpb-407.9640153.33885-7.6497.70e-14\*\*\*El evFt-0.073850.01726-4.2792.17e-05\*\*\*

- Again, stand characteristics very important
- Predicting site productivity (ft<sup>3</sup>/acre/year) is difficult
  - Particularly when only using site variables
    - Climate, topography, soils
- Other measures of productivity?

Response variables

Largest 10 trees per plot
Volume growth
Largest 10 DF per plot
Height growth
Diameter growth

Include one stand explanatory variable

• QMD

- 10 Largest trees per plot
  - Diameter growth R<sup>2</sup> = 0.55





- 10 Largest trees per plot
  - Volume growth  $R^2 = 0.77$

Response: mean. dom. vg. yr					
	Sum Sq	Df	F value	<b>Pr(&gt;F)</b>	
El evFt	7.745	1	35.035	7. 933e-09	* * *
Mat	5. 585	1	25.266	8. 104e-07	* * *
qmd	206. 962	1	936. 228	< 2. 2e-16	* * *
logit. shade	2.359	1	10.673	0. 001199	* *
Resi dual s	74.939	339			



- 10 fastest height growing trees
  - Volume growth  $R^2 = 0.30$

Response: fast. mean. vg. yr Df Sum Sq F value Pr(>F)(Intercept) 280.2 40.7850 3.042e-10 1 \* \* \* qmd 2031.1 1 295.5997 < 2.2e-16\* \* \* qmd: AshClass 105.7 2 7.6893 0.0004962 \* \* \* Resi dual s 4961.0 722



AshClass

## Conclusions

- Total stand site productivity is challenging to predict / model
  - Stand characteristics are important
- Looking at certain trees or classes in a stand could be representative of a site productivity
- Productivity of a class can be predicted fairly accurately with only a few site variables
  - Largest 10 trees
- Continue to look at volume growth as a measure of site productivity



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# Questions?

