## Toward Developing a Regional IFC Forest Productivity Model



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## Summary

- Background
- Individual tree analysis
- RF
- Linear models
- Whole stand productivity
- Stand subset productivity
- Challenges
- Conclusions / future directions


## Background

- What is Site Productivity?
- Productivity can be directly measured
- Volume growth/acre/year
- Site Productivity is a little more tricky . . .
- Volume growth/acre/year the site is capable of producing
- Difficult to directly measure



## Background

- Proxies are often used for site productivity
- Site index
- Habitat type
- Site productivity is very useful
- Growth and yield models
- Land appraisals
- Management strategies



## Background

Growth and Yield Models

- Many use individual tree models
- Diameter growth
- Volume growth
- FVS
- Whole stand models
- Less common
- Ultimate goal of G \& Y models


## The Dataset

- Repeated growth measurements (CFI)
- Primarily Northern ID
- Variety of owners
- USFS
- IDL
- Potlatch
- Etc.


Figure 1: Sample plot locations

## The Dataset

- 4589 Unique Stands / Plots
- Over 1,000,000 Individual tree observations
- Initially ...
- Much is lost after data screening


Figure 1: Sample plot locations

## Phase 1: Individual Tree

- Response Variable
- InDDS
- "...Logarithm of the change in squared insidebark individual tree diameter over a period of 10 years..."
- Used in FVS
- 110,852 individual tree observations
- Model selection methods
- Random Forests (RF, Breiman 2001)
- Best $\mathrm{R}^{2}$


## Random Forests Models

- Builds multiple regression trees
- Rank explanatory variables on influence / importance
- Examines:
- Increase in Mean Squared Error
- Node purity
- Decrease in residual sum of squares
- Averaged over all the trees


## Random Forests Models

## Four models

- rf1: all predictors were included
- rf2: just site predictors
- rf3: rf2 plus Species and cr.
- rf4: traditional variables used in FVS

Table 9: Summary of the RF models

| RF model | R2 | Best 10 predictors |
| :---: | :---: | :--- |
| rf1 | 0.84 | DBH, cr, Species, soilcd, TopHt, baldbh, QMD, pratio, BAPctile, Slope |
| rf2 | 0.39 | slca, slsa, soilcd, pratio, ffp, smrsprpb, map, Geology, gsp, winp |
| rf3 | 0.54 | Species, cr, pratio, slca, slsa, winp, soilcd, map, adi, Geology |
| rf4 | 0.83 | cr, Species, DBH, TopHt, elev, slca, baldbh, BAPctile, QMD, PtBAL |

## RF 1

- rf1: all predictors were included

| Variable | Description |
| :---: | :--- |
| DBH | Diameter breast height |
| Species | Tree species |
| cr | Crown ratio |
| soilcd | Soil class names |
| pratio | Ratio of summer precipitation to total precipitation |
| TopHt | Height of the largest 40 trees per acre in the stand |
| baldbh | Interaction between DBH and Ratio of basal area in trees larger than <br> subject tree (bal) |
| QMD | Quadratic mean diameter |
| BAPctile | Percentile point in the distribution of tree basal areas |
| Slope | Slope percentage |

Table 9: Summary of the RF models
RF model R2 Best 10 predictors
rf1 0.84 DBH, cr, Species, soilcd, TopHt, baldbh, QMD, pratio, BAPctile, Slope

## Phase 1: Individual Tree

## Explanatory Variables

- Species

Table 1: Species codes, names, and observation counts

| FVSCode | Common Name | Name | Frequency |
| :---: | :--- | :--- | ---: |
| AF | subalpine fir | Abies lasiocarpa | 3085 |
| DF | Douglas-fir | Pseudotsuga menziesii | 24769 |
| ES | Engelmann spruce | Picea engelmannii | 3383 |
| GF | grand fir | Abies grandis | 23314 |
| LP | lodgepole pine | Pinus contorta | 5520 |
| MH | mountain hemlock | Tsuga mertensiana | 1986 |
| PP | ponderosa pine | Pinus ponderosa | 2477 |
| RC | western redcedar | Thuja plicata | 13465 |
| WH | western hemlock | Tsuga heterophylla | 8686 |
| WL | western larch | Larix occidentalis | 7481 |
| WP | western white pine | Pinus monticola | 16701 |

## Phase 1: Individual Tree

## Soil class names (soilcd)

Table 2: Soil class names (soilcd) and observation counts
Soil class name Frequency
Basalt155
Glacial ..... 1427
Loess ..... 261
LoessBasalt ..... 803
LoessMetaGranite ..... 1001
Metased ..... 426
Other ..... 331
Seds ..... 1180
VolcanicBasalt ..... 166
VolcanicGlacial ..... 7901
VolcanicLoess ..... 2696
VolcanicLoessBasalt ..... 2814
VolcanicLoessGlacial ..... 8156
VolcanicLoessMetaGranite ..... 3540
VolcanicLoessMetased ..... 523
VolcanicLoessOther ..... 239
VolcanicLoessQuartzite ..... 1209
VolcanicMetaGranite ..... 16208
VolcanicMetased ..... 41667
VolcanicOther ..... 408
VolcanicQuartzite ..... 4919
VolcanicSeds ..... 14822

## RF2

- rf2: just site predictors

| Variable | Description |
| :--- | :--- |
| slca | Slope ${ }^{*} \cos \left(\mathrm{pi} / 180^{*}\right.$ Aspect) |
| slsa | Slope $* \sin \left(\mathrm{pi} / 180^{*}\right.$ Aspect) |
| soilcd | Soil class names |
| pratio | Ratio of summer precip to total precip |
| ffp | Frost free period |
| smrsprpb | Summer spring precipitation balance |
| winp | Winter precipitation |
| map | Mean annual precipitation |
| Geology | Parent material |
| gsp | Growing season precipitation |

Table 9: Summary of the RF models
RF model R2 Best 10 predictors
rf2 0.39 slca, slsa, soilcd, pratio, ffp, smrsprpb, map, Geology, gsp, winp

## RF 3

- rf3: rf2 plus Species and cr.

| Variable | Description |
| :--- | :--- |
| slca | Slope * cos(pi/180*Aspect) |
| Species | Tree species |
| cr | Crown ratio |
| slsa | Slope * sin(pi/180*Aspect) |
| soilcd | Soil class names |
| pratio | Ratio of summer precip to total precip |
| winp | Winter precipitation |
| map | Mean annual precipitation |
| Geology | Parent material |
| adi | Annual dryness index |

Table 9: Summary of the RF models

## RF 3

## - Geology

Table 3: Geology variable frequencies

| Geology | Frequency |
| :--- | ---: |
| CaMetased | 24464 |
| Extrusive | 4895 |
| Glacial | 10497 |
| Intrusive | 18375 |
| Metasedimentary | 44045 |
| Other | 8467 |
| Sedimentary | 109 |

Table 9: Summary of the RF models

| RF model R2 | Best 10 predictors |  |
| :---: | :--- | :--- |
| rf3 | 0.54 | Species, cr, pratio, slca, slsa, winp, soilcd, map, adi, Geology |

## RF 4

## rf4: traditional variables used in FVS

| Variable | Description |
| :--- | :--- |
| DBH | Diameter breast height |
| slca | Slope * $\cos \left(\mathrm{pi} / 180^{*}\right.$ Aspect) |
| Species | Tree species |
| cr | Crown ratio |
| TopHt | Height of the largest 40 trees per acre in the stand |
| elev | Elevation |
| baldbh | Interaction between DBH and Ratio of basal area in trees <br> larger than subject tree (bal) |
| QMD | Quadratic mean diameter |
| BAPctile | Percentile point in the distribution of tree basal areas |
| PtBAL | Basal area per acre in larger trees measured on the <br> subplot same as BAL if there is one plot |

Table 9: Summary of the RF models
RF model R2 Best 10 predictors
rf4 0.83 cr, Species, DBH, TopHt, elev, slca, baldbh, BAPctile, QMD, PtBAL

## RF Model Summary



## Phase 2: Individual Tree

- Linear and mixed effects models
- Selected based on RF models
- Best model $\mathrm{R}^{2}$
- 2 best models presented here

Table 11: Two sequences of adding variables to the lme models[ R2 is reported without random effect
R2 Predictors
Sequence 1, adding tree metrics
0.65 Species + soilcd + Species:cr + slca + slsa + pratio + map + Species:adi +
$I(\log (\mathrm{DBH}))+\mathrm{I}(\mathrm{DBH} * \mathrm{DBH})+\mathrm{bal}+\mathrm{Species}: \mathrm{baldbh}$
Sequence 2, adding site metrics
0.64 Species + Species:cr + I(log(DBH)) + I(DBH*DBH) + bal + Species:baldbh + soilcd + slca + slsa + pratio + map

## Phase 2: Individual Tree



Itrie2.1


Table 10: Pseudo-R-square (R2) values for the linear models in table 8

| Linear model | R2 | R2 when predictions include random <br> "StandID" effect |
| :--- | :--- | :--- |


| $\operatorname{lm} 1$ | 0.23 | $\mathrm{n} / \mathrm{a}$ |
| :---: | :---: | :---: |
| $\operatorname{lm} \mathrm{e} 1$ | 0.10 | 0.48 |
| $\operatorname{lm} 2$ | 0.69 | $\mathrm{n} / \mathrm{a}$ |
| $\ln 22$ | 0.65 | 0.82 |
| $\operatorname{lme} 3$ | 0.64 | 0.82 |
| $\operatorname{lme} 4$ | 0.64 | 0.82 |

- All models tested here
- Random "StandID" effect explaining a lot of variation
- Not explained by other variables


## Individual Tree Conclusions

- Growth models can benefit from including soil and climate data
- Stand and tree characteristics often out-weight site characteristics
- Site characteristics are indirectly incorporated in stand and tree measurements
- Quantifying inter-tree competition was difficult on large fixed area plots
- "StandID" effect?
- Whole stand productivity could be explored. . .


## Whole Stand Productivity

- Same data set
- Summarized and examined in different ways
- 4,308 stands initially
- $12 \%-20 \%$ available after screening
- Stands that were treated with fertilizer
- Negative or 0 growth


## Whole Stand Productivity

Data Summaries

- DBH, Height, Volume calculated for every tree
- Every measurement period
- Expanded to a per acre value
- Means for each stand to represent productivity
- Standardized to per year
- Different measurement period lengths


## Whole Stand Productivity

Model and Variable selection

- 3 parts
- First chose model with the best fit via AICC selection
- Removed insignificant variables $(\alpha<0.1)$
- Tested interactions between significant variables


## Whole Stand Productivity

- Whole stand volume growth (ft ${ }^{3} /$ acre/year)
- Including everything . . . $\mathrm{R}^{2}=0.56$ !

|  |  | Df | al ue |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| nt er cept) | 571 | 1 | 0. 2718 | 0. 6024906 |  |
| El evFt | 32129 | 1 | 15. 2918 | 0. 0001115 |  |
| cub.ft.ac | 70483 | 1 | 33.5467 | 1. 599e-08 |  |
| qnd | 38516 | 1 | 18. 3319 | 2. $425 \mathrm{e}-05$ |  |
| I ogit. shade | 8338 | 1 | 3. 9684 | 0. 0471717 |  |
| El evFt : DEM SI opeP | 21862 |  | 10. 4052 | 0. 0013802 |  |
| DEM SI opePct:tp. acre | 27307 | 1 | 12. 9969 | 0. 0003593 |  |
| cub.ft. acre: SI opePct | 36598 |  | 17. 4190 | 3. $823 \mathrm{e}-05$ |  |
| cub.ft.acre: DF_SI | 92848 |  | 44. 1915 | 1. 205e-10 |  |
| cub.ft.acre:tp.ac | 19223 | 1 | 9. 1494 | 0. 0026797 |  |
| qrod: Mat | 12258 | 1 | 5. 8341 | 0. 0162520 |  |
| qnad: DEM SI opePct | 30280 |  | 14. 4120 | 0. 0001742 |  |
| DEM SI opePct: curt.rd | 10578 | 1 | 5. 0347 | 0. 0254955 |  |
| DF_SI : curt.rd | 94144 |  | 44. 8085 | 9. 125e-11 |  |
| cub.ft.acre: cur | 46801 |  | 22. 275 | 3. $472 \mathrm{e}-06$ |  |
| qnod: curt.rd | 33538 | 1 | 15. 9626 | 7. 942e- 05 |  |
| DF_SI : sdi | 104879 |  | 49. 9178 | 9. 293e-12 |  |
| cub.ft.acre: sdi | 44641 |  | 21. 2471 | 5. 743e-06 |  |
| I ogit. shade: Mat | 16244 | 1 | 7. 7316 | 0. 0057323 |  |
| El evFt: I ogit.shad | 7880 | 1 | 3. 7506 | 0. 0536270 |  |
| qud: I ogit. shade | 21468 | 1 | 10. 2178 | 0. 0015230 |  |
| I ogit. shade: curt.rd | 26262 | 1 | 12. 4995 | 0. 0004642 |  |
| I ogit. shade: sdi | 25508 | 1 | 12. | 0005587 |  |
| Resi dual s | 705946 |  |  |  |  |

## Whole Stand Productivity

- Got a little messy
- Just look at site factors . . . $\mathrm{R}^{2}=0.09$

|  | Esti mate | Std. Error | val ue | $\operatorname{Pr}(>\|t\|)$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ( I nt er cept) | 1000. 98241 | 162. 98553 | 6. 142 | 1. $45 \mathrm{e}-09$ |  |
| dd5 | - 0.29277 | 0. 05517 | -5. 306 | 1. 55e- 07 | *** |
| smspr pb | - 407. 96401 | 53. 33885 | -7. 649 | 7. 70e-14 |  |
| El evFt | -0.07385 | 0. 01726 | -4. 279 | 2. $17 \mathrm{e}-05$ |  |

- Again, stand characteristics very important
- Predicting site productivity (ft³/acre/year) is difficult
- Particularly when only using site variables
- Climate, topography, soils
- Other measures of productivity?


## Other Measures of Site Productivity

Response variables

- Largest 10 trees per plot $\longrightarrow$ • Volume growth
- Largest 10 DF per plot $\longrightarrow \bullet$ Height growth
- Diameter growth
- Fastest 10 growing trees (height)

Include one stand explanatory variable

- QMD


## Other Measures of Site Productivity

- 10 Largest trees per plot
- Diameter growth $\mathrm{R}^{2}=0.55$

Response: mean. dom dg. yr




## Other Measures of Site Productivity

- 10 Largest trees per plot
- Volume growth $\mathrm{R}^{2}=0.77$

Response: mean. domvg. yr

|  | Sum Sq | Df | F val ue | $\operatorname{Pr}(>F)$ |  |
| :--- | ---: | ---: | ---: | ---: | :---: |
| El evFt | 7.745 | 1 | 35.035 | $7.933 \mathrm{e}-09$ | $* * *$ |
| Mat | 5.585 | 1 | 25.266 | $8.104 \mathrm{e}-07$ | $* * *$ |
| qrad | 206.962 | 1 | 936.228 | $<2.2 \mathrm{e}-16$ | $* * *$ |
| I ogit. shade | 2.359 | 1 | 10.673 | $0.001199^{* *}$ |  |
| Resi dual s | 74.939 | 339 |  |  |  |



## Other Measures of Site Productivity

- 10 fastest height growing trees
- Volume growth $\mathrm{R}^{2}=0.30$

Response: fast. mean. vg. yr

|  | Sum Sq | Df | F val ue | $\operatorname{Pr}(>F)$ |  |
| :--- | ---: | ---: | ---: | :---: | :---: |
| ( I nt er cept ) | 280.2 | 1 | 40.7850 | $3.042 \mathrm{e}-10$ | $* * *$ |
| qnd | 2031.1 | 1 | 295.5997 | $<2.2 \mathrm{e}-16$ | $* * *$ |
| qnd: AshCl ass | 105.7 | 2 | 7.6893 | $0.0004962 * * *$ |  |
| Resi dual s | 4961.0 | 722 |  |  |  |



## Conclusions

- Total stand site productivity is challenging to predict / model
- Stand characteristics are important
- Looking at certain trees or classes in a stand could be representative of a site productivity
- Productivity of a class can be predicted fairly accurately with only a few site variables
- Largest 10 trees
- Continue to look at volume growth as a measure of site productivity


## Acknowledgements

- Mark Coleman, Mark Kimsey, Terry Shaw for guidance and funding
- Cooperators for providing the wealth of data
- Nick Crookston for the report and hard work


## Questions?

